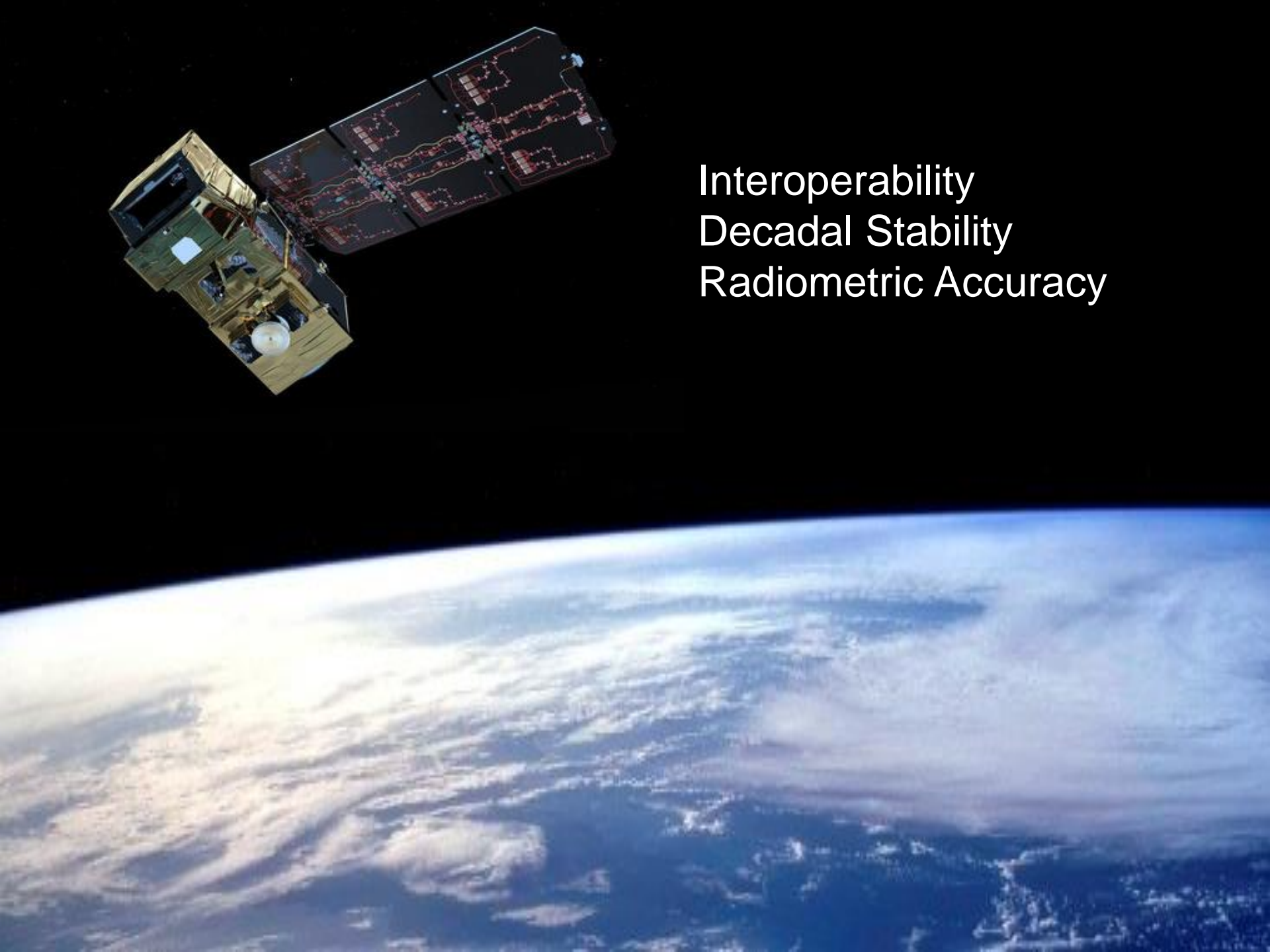


Metrology Principles for Earth Observation: the NMI view

Emma Woolliams
17th October 2017



Interoperability
Decadal Stability
Radiometric Accuracy



- Identical worldwide
- Century-long stability
- Absolute accuracy

Organisation of World Metrology



- The Convention of the Metre
(*Convention du Mètre*)

1875

- International System of Units (SI)
(*Système International d'Unités*)

1960

- Mutual Recognition Arrangement
(CIPM-MRA)

1999



Bureau

International des

Poids et

Mesures

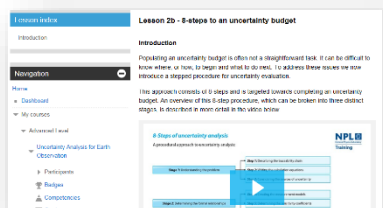
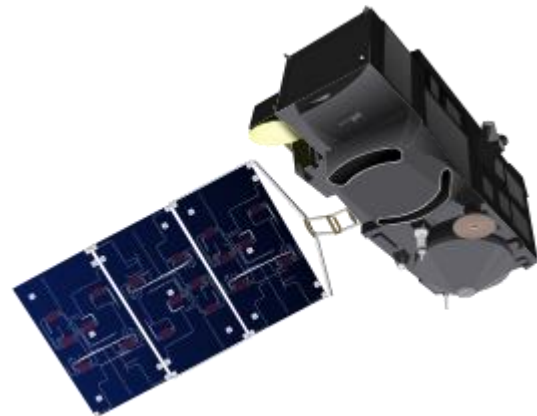
This presentation



1. How world metrology achieves interoperability, stability and accuracy

2. How these principles can be applied to Earth Observation

3. Resources to help



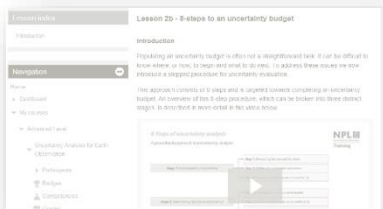
This presentation



1. How world metrology achieves interoperability, stability and accuracy

2. How these principles can be applied to Earth Observation

3. Resources to help





- How do we make sure a wing built in one country fits a fuselage built in another?
- How do we make sure the SI units are stable over centuries?
- How do we improve SI over time without losing interoperability and stability?

History of the metre

1795



1 ten millionth of the distance from the North Pole to the Equator through Paris

1799

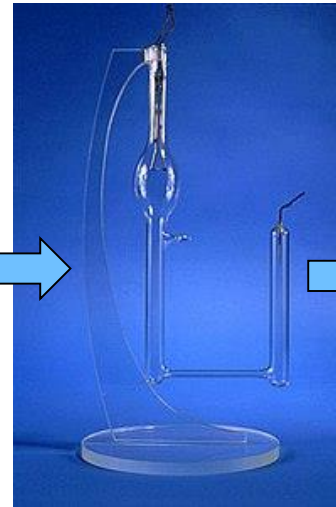
Metre des Archives

1889

International Prototype



1960

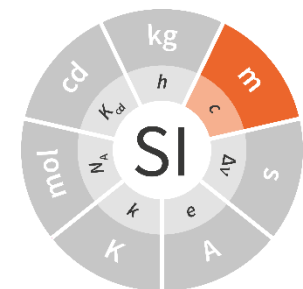


1 650 763.73 wavelengths of a krypton-86 transition

1983

Distance light travels in 1/299 792 458th of a second

2018



Distance that makes the speed of light 299 792 458 m s⁻¹

- Stable
- Improves over time
- Reference to physical process

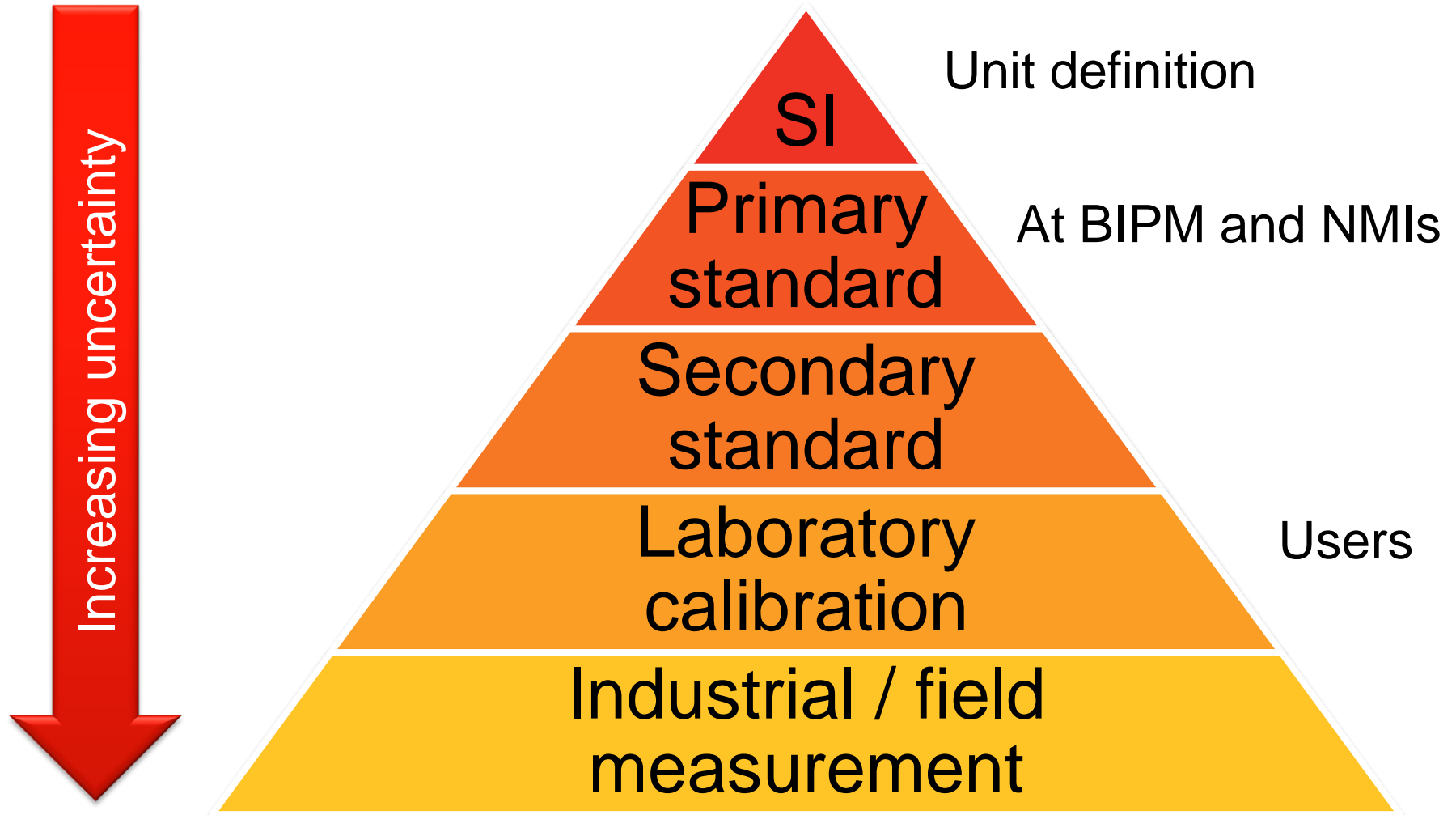
Three principles

Traceability

Uncertainty Analysis

Comparison

Traceability





Traceability: An unbroken chain

Transfer
standards

Audits

SI

Rigorous
uncertainty
analysis

Documented
procedures

Rigorous Uncertainty Analysis



First edition September 2008

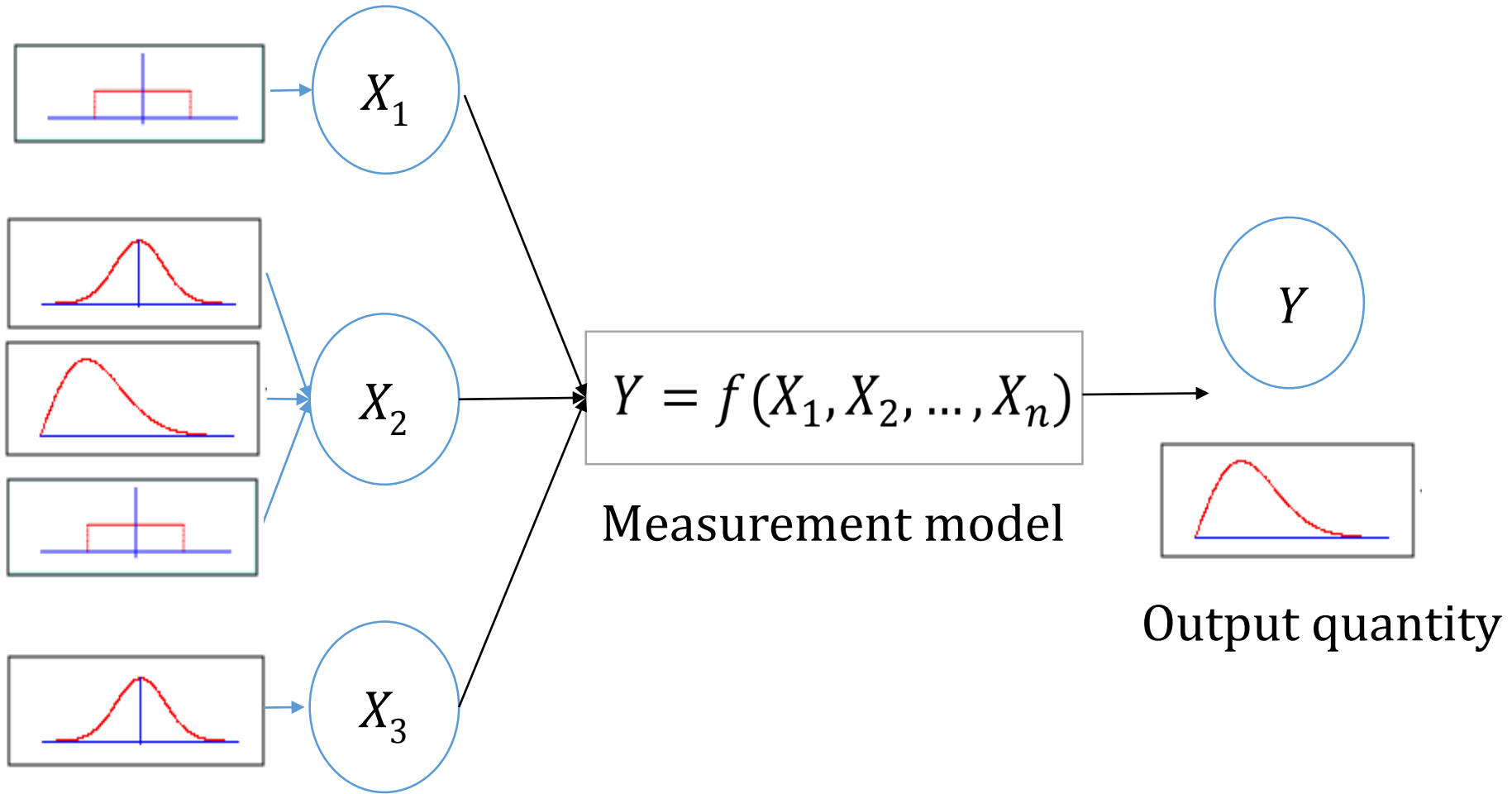
© JCGM 2008

The Guide to the expression of Uncertainty in Measurement (GUM)

- The foremost authority and guide to the expression and calculation of uncertainty in measurement science
- Written by the BIPM, ISO, etc.
- Covers a wide number of applications
- Also a set of supplements

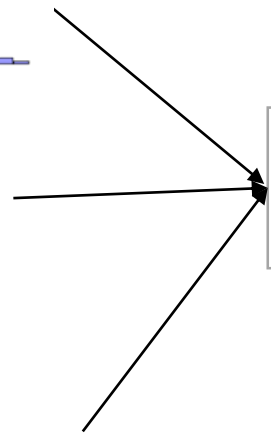
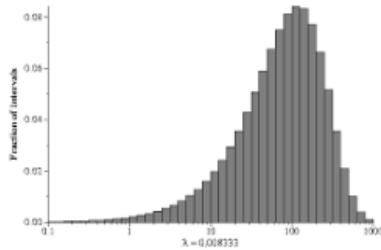
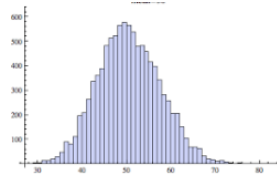
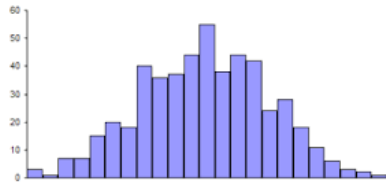
<http://www.bipm.org/en/publications/guides/gum.html>

Principle of Uncertainty Analysis



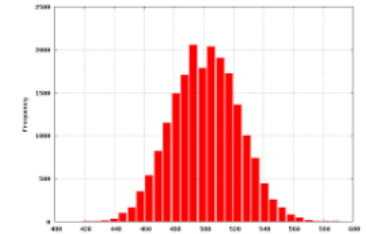
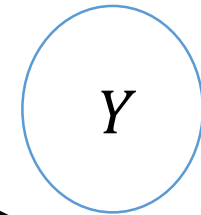
Error effects Input quantities

Monte Carlo Approach



$$Y = f(X_1, X_2, \dots, X_n)$$

Measurement model



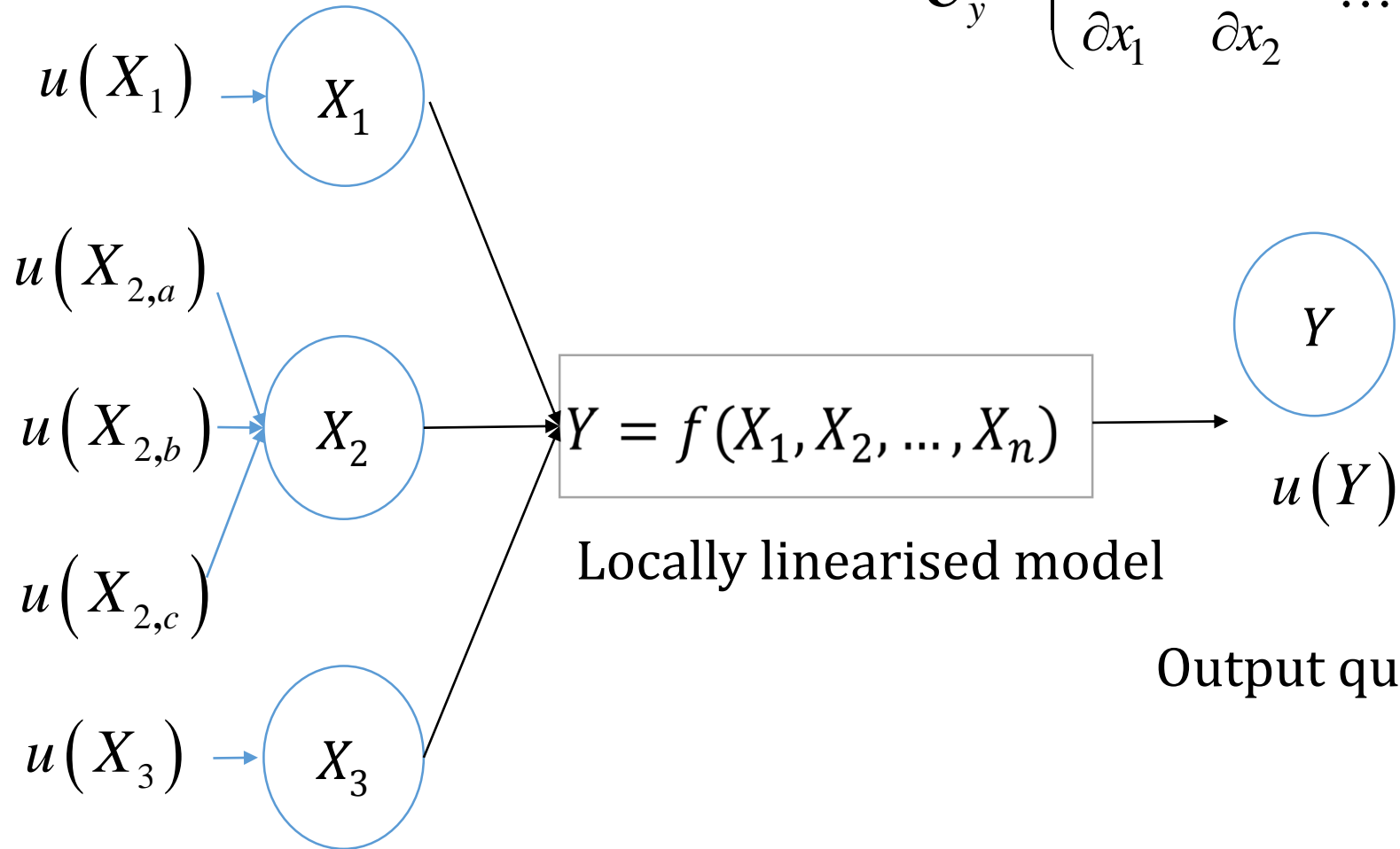
Output quantity

Error effects Input quantities

Law of Propagation of Uncertainty

$$u^2(y) = \mathbf{C}_y \mathbf{U}_x \mathbf{C}_y^\top$$

$$\mathbf{C}_y = \begin{pmatrix} \frac{\partial f}{\partial x_1} & \frac{\partial f}{\partial x_2} & \dots & \frac{\partial f}{\partial x_n} \end{pmatrix}$$



Error effects Input quantities

Output quantity

Comparisons

Scientific comparisons:

Immature field – learning what we don't know

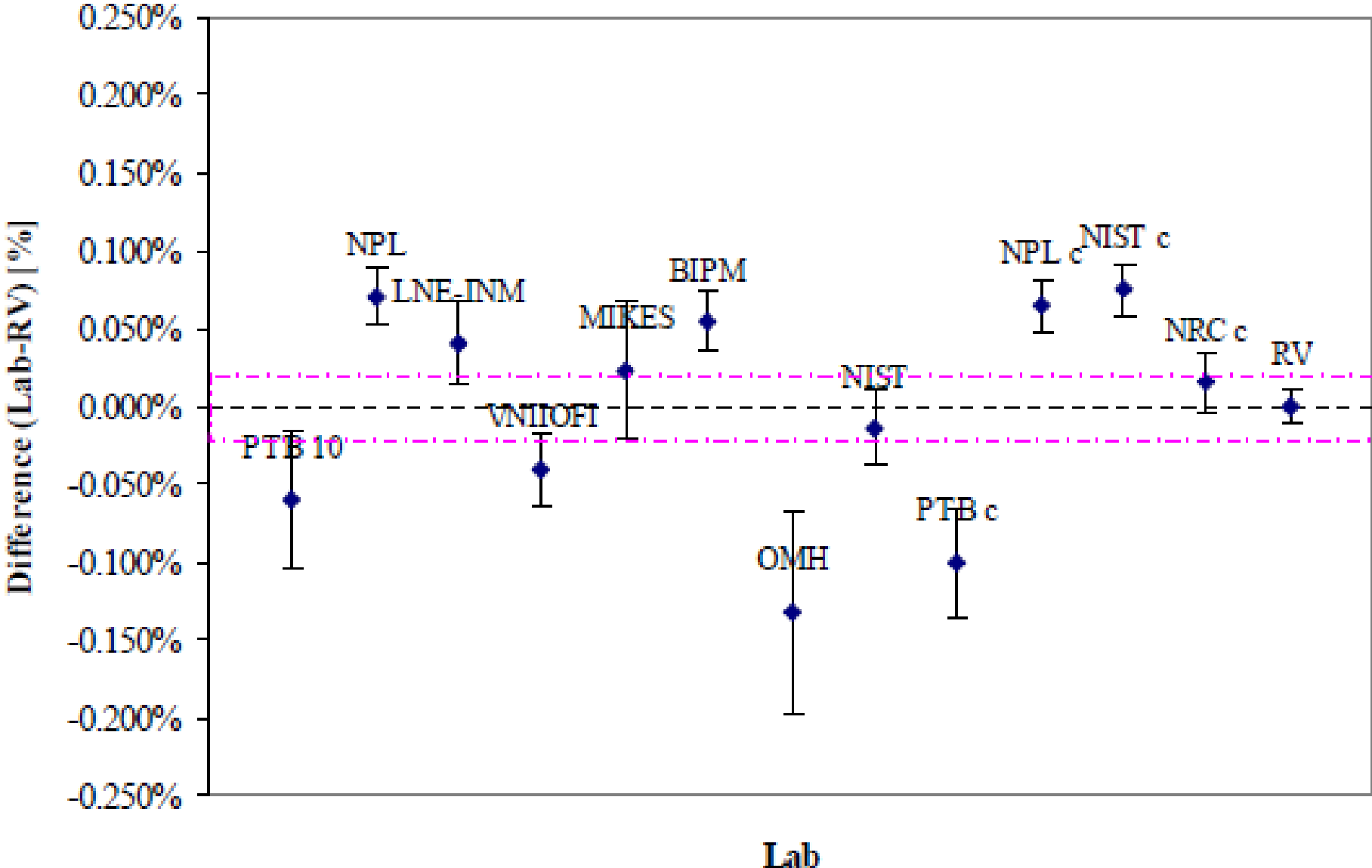
Formal MRA comparisons:

Mature field – to check world metrology still works!



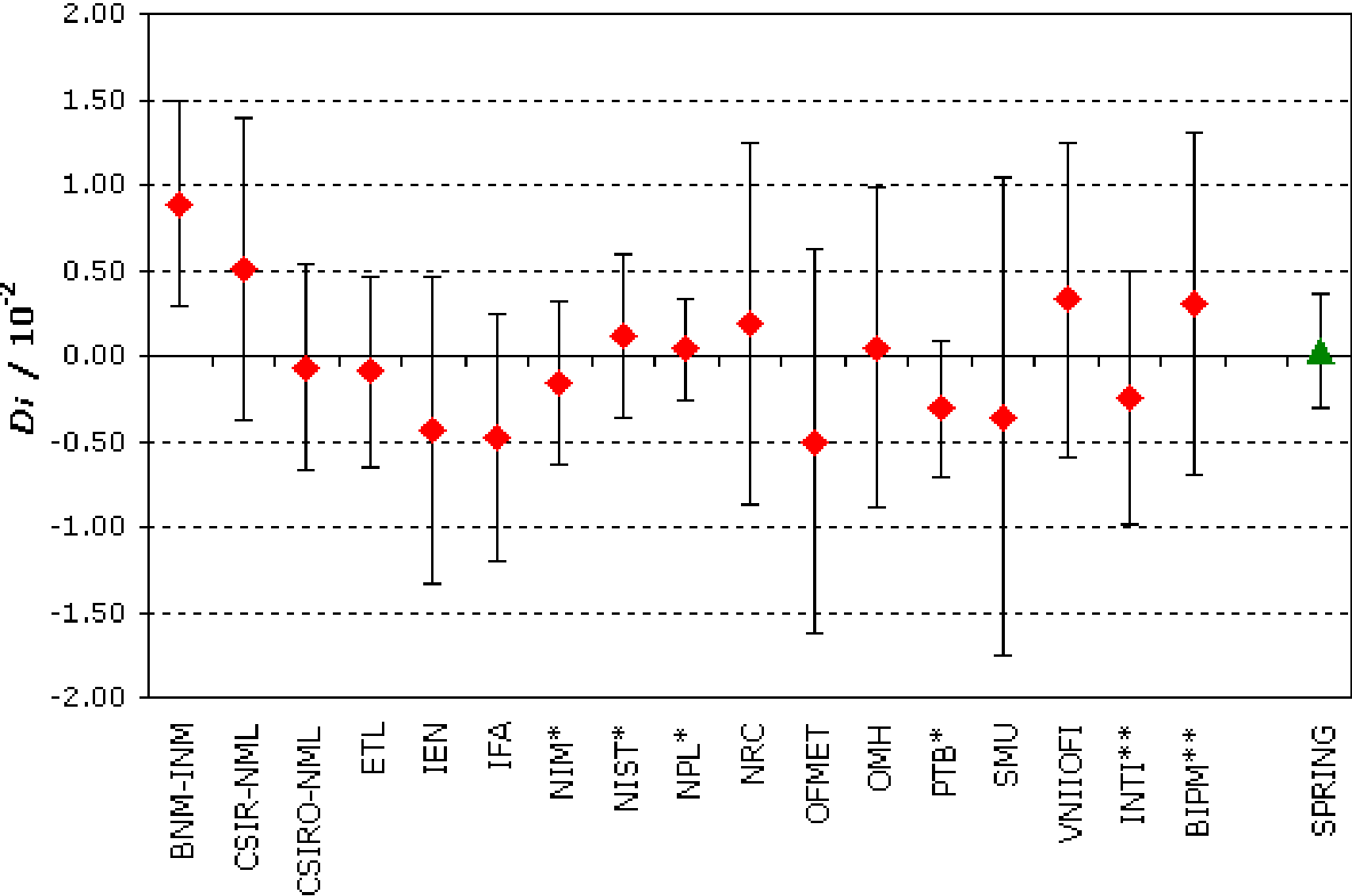
Lab-to-lab

(results of a scientific comparison)



MRA Formal comparison

Luminous Intensity key comparison

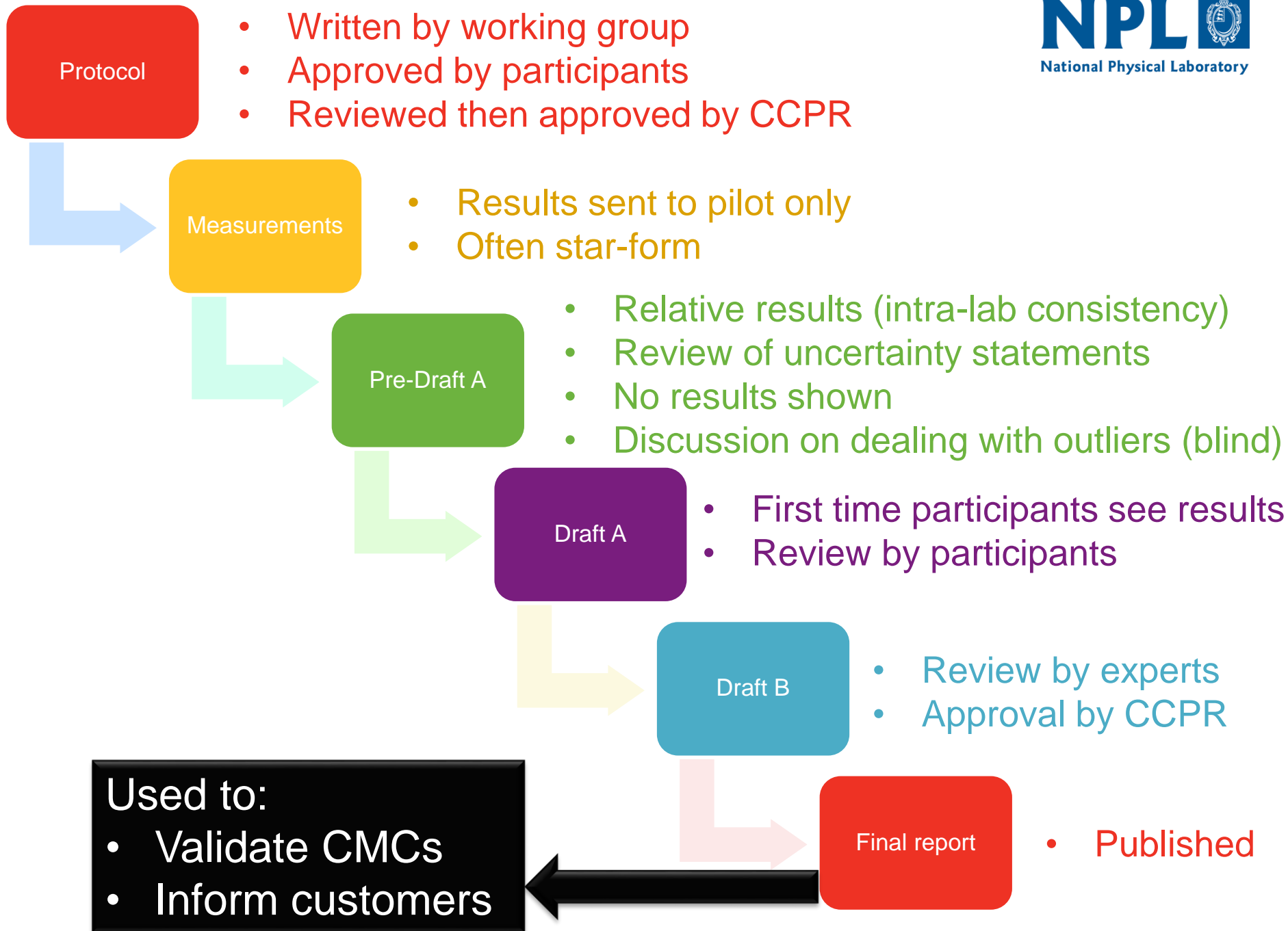


CMC Database

- <https://kcdb.bipm.org/>
- Evidence: Formal peer review or audit of procedures, participation in a relevant key comparison (within 10 years) with declared uncertainties defended, review within region and between regions

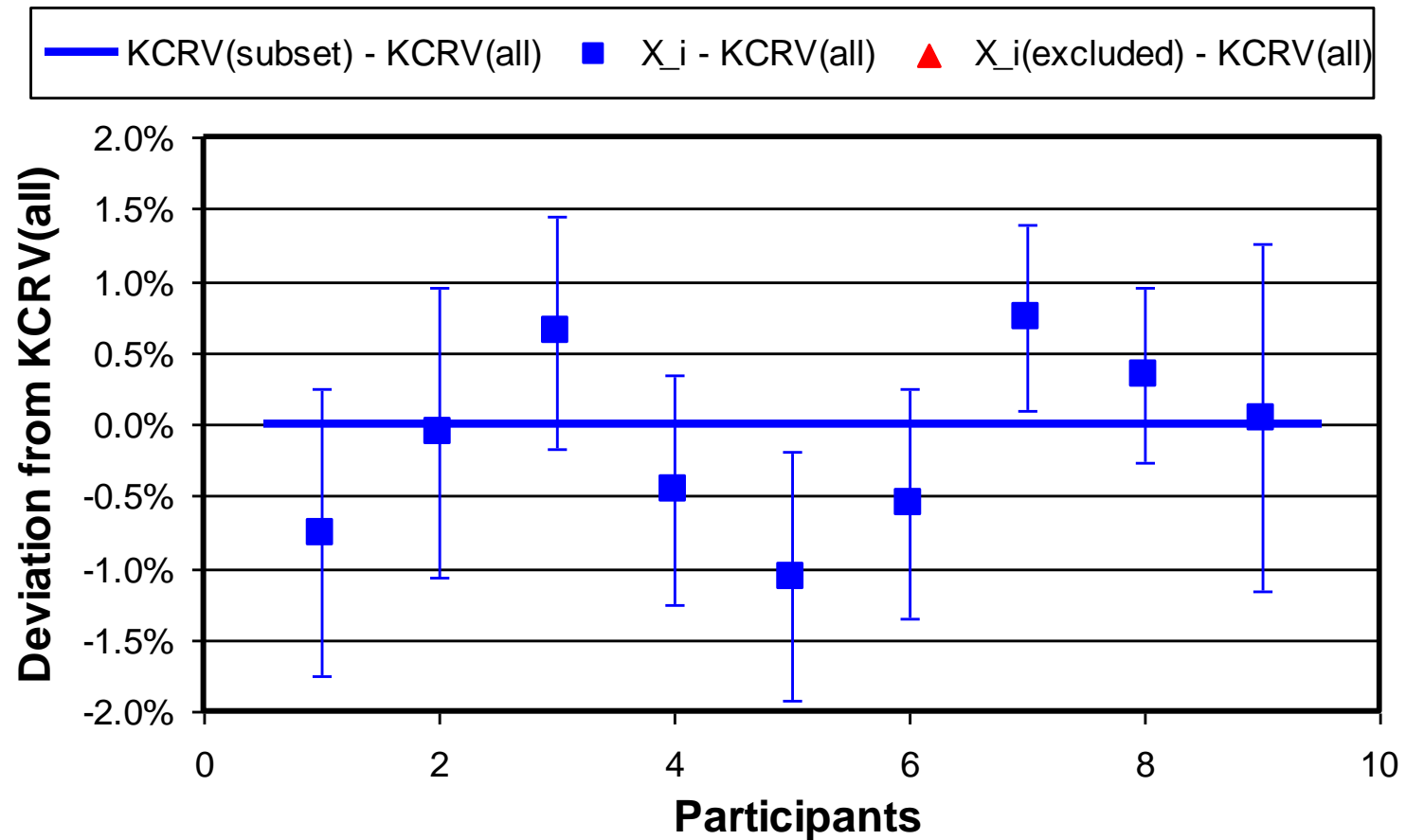
Irradiance, spectral. Tungsten lamp, **$6E-03$ (W/m²)/nm to 0.27 (W/m²)/nm**
Relative expanded uncertainty ($k = 2$, level of confidence 95%) in %: **0.9 to 0.8 (with wavelength)**
Spectroradiometer
Wavelength: 500 nm to 800 nm
Bandwidth: < 20 nm
Other types of source can also be measured
Approved on 20 April 2017

Irradiance, spectral. Tungsten lamp, **$1.5E-03$ (W/m²)/nm to 0.29 (W/m²)/nm**
Relative expanded uncertainty ($k = 2$, level of confidence 95%) in %: **0.5**
Spectroradiometer
Wavelength: 801 nm to 1600 nm
Bandwidth: < 20 nm
Other types of source can also be measured
Approved on 20 April 2017



Ongoing research: Outliers

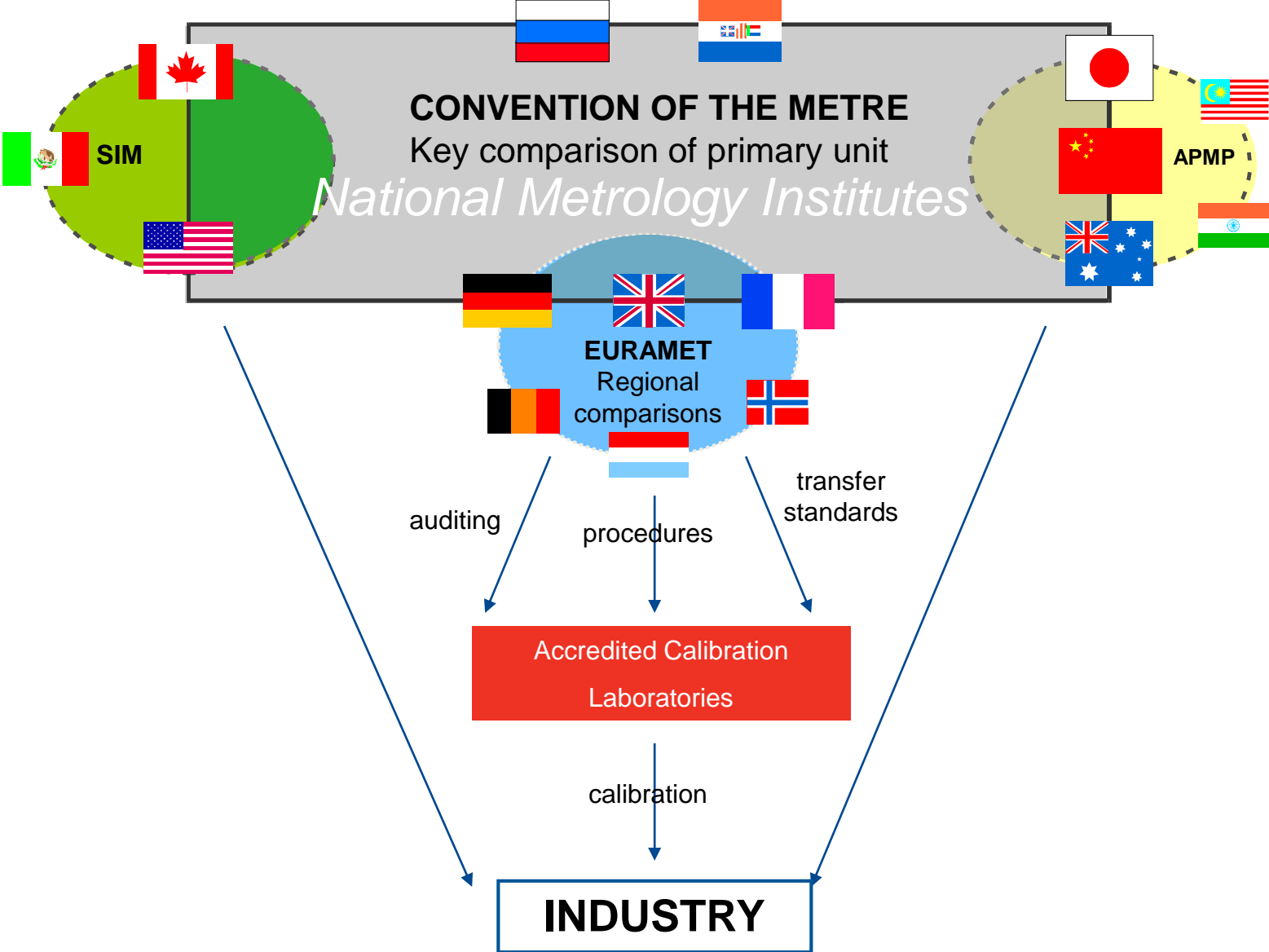
Error bars: expanded unc. ($k = 2$)



χ^2_{obs}	20.5
$\chi^2_{0.05}(\nu)$	15.507

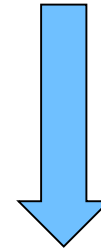
If you exclude 5 or 7 the others (including 7 or 5) become consistent

Mutual Recognition Arrangement





- Identical worldwide
- Century-long stability
- Absolute accuracy



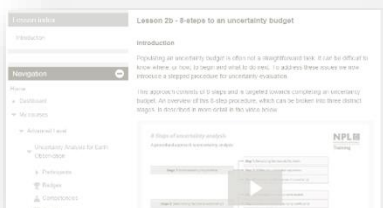
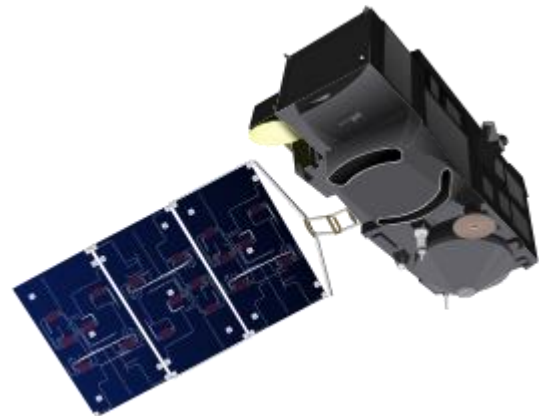
- Achieved through:
- Traceability
 - Uncertainty Analysis
 - Comparison

This presentation



1. How world metrology achieves interoperability, stability and accuracy

2. How these principles can be applied to Earth Observation



3. Resources to help

The traceability chain is broken



**No repeat
measurements**



No reference in
space ...



No reference in
space ... yet

TRUTHS



www.npl.co.uk/truths

Three principles

Traceability

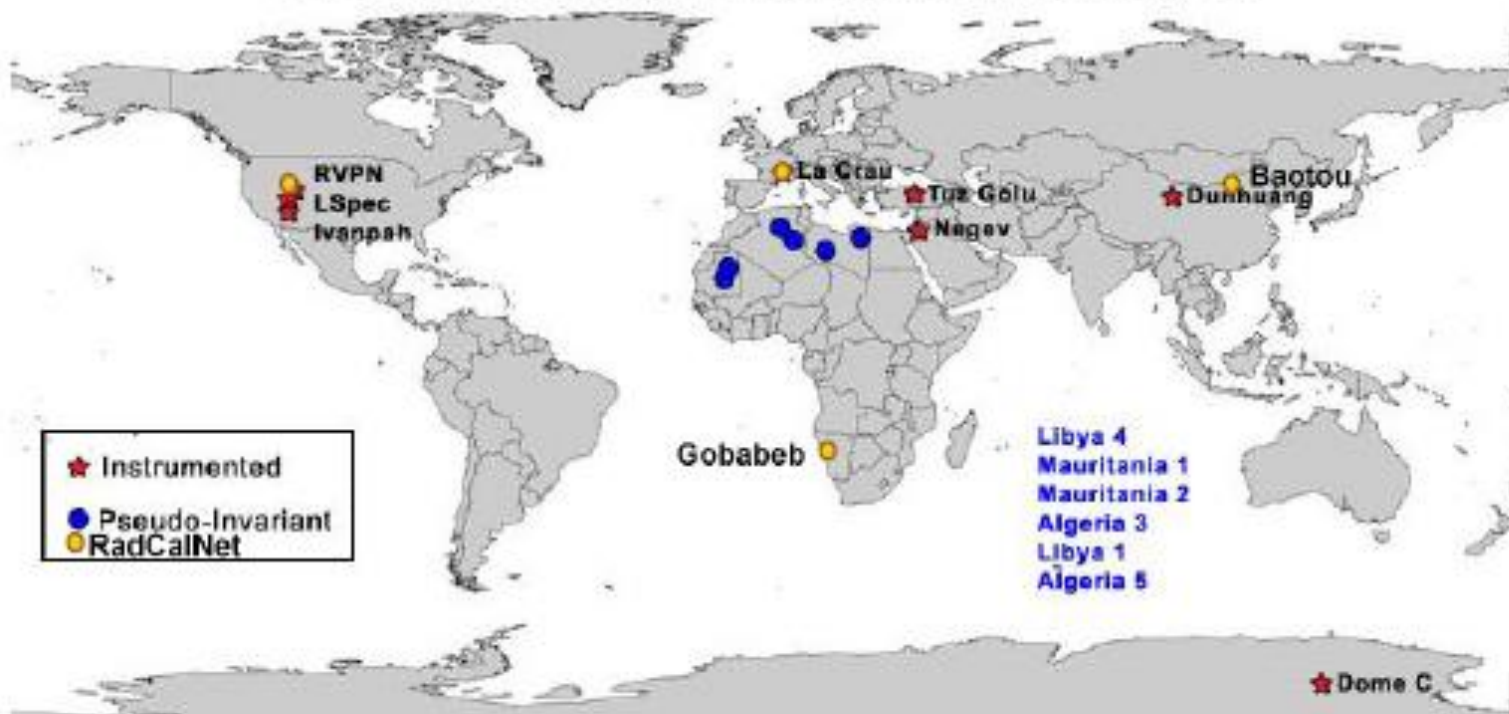
Uncertainty Analysis

Comparison

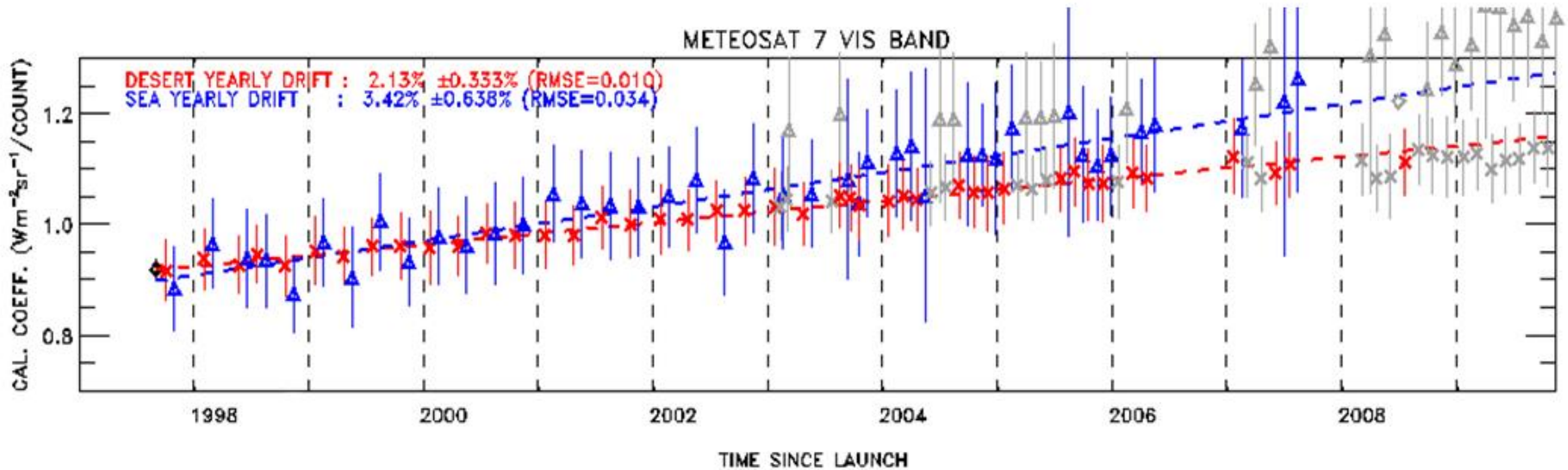
Traceability



CEOS Reference Standard Tests Sites



Traceability: Using reference sites



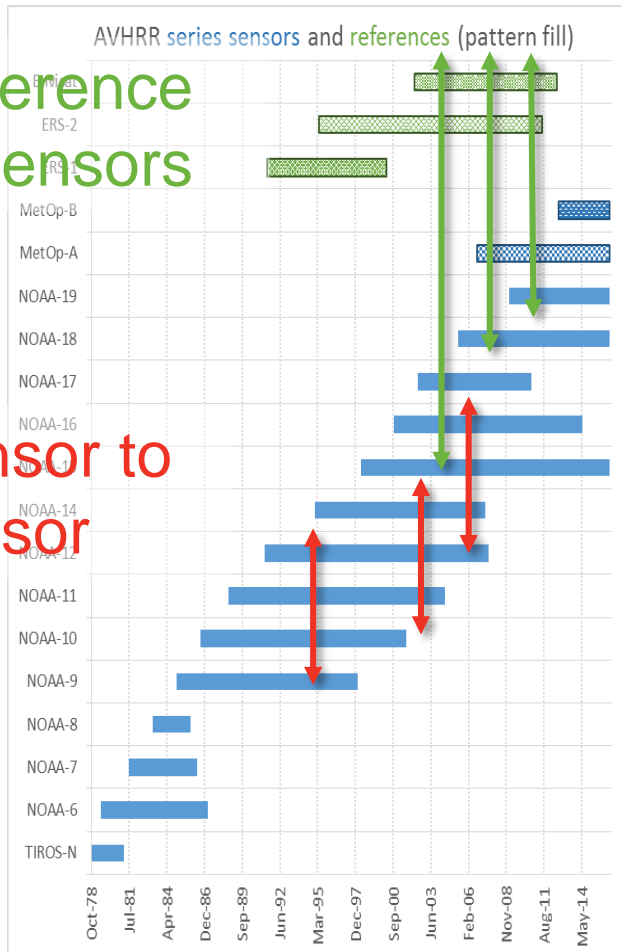
Drift of MVIRI Vis band since launch as determined from desert (red) and ocean (blue) test sites. Figure from:

<https://scienceblog.eumetsat.int/2016/11/improving-climate-data-records-with-fiduceo/>

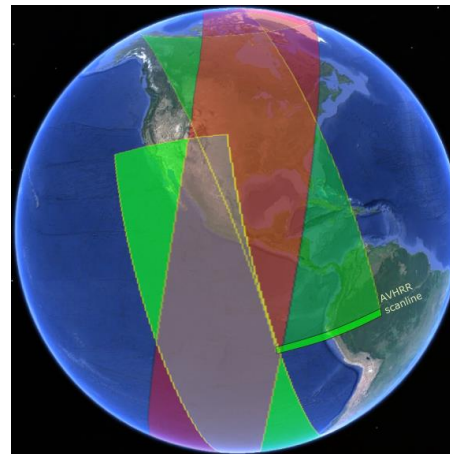
Traceability

Reference
to sensors

Sensor to
sensor

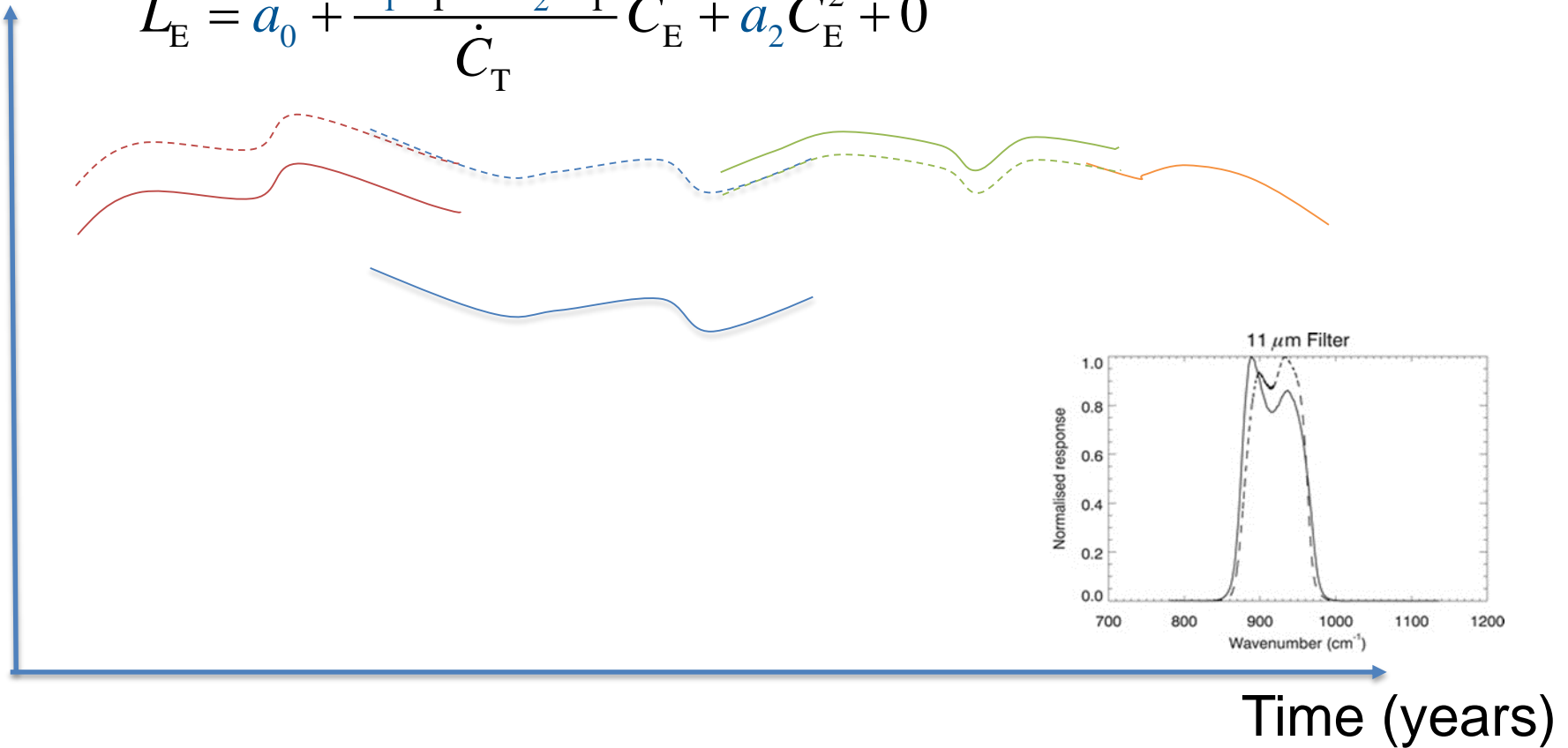


- Reference radiance, or sensor-to-sensor
- Many (150 million +)
- Correlated

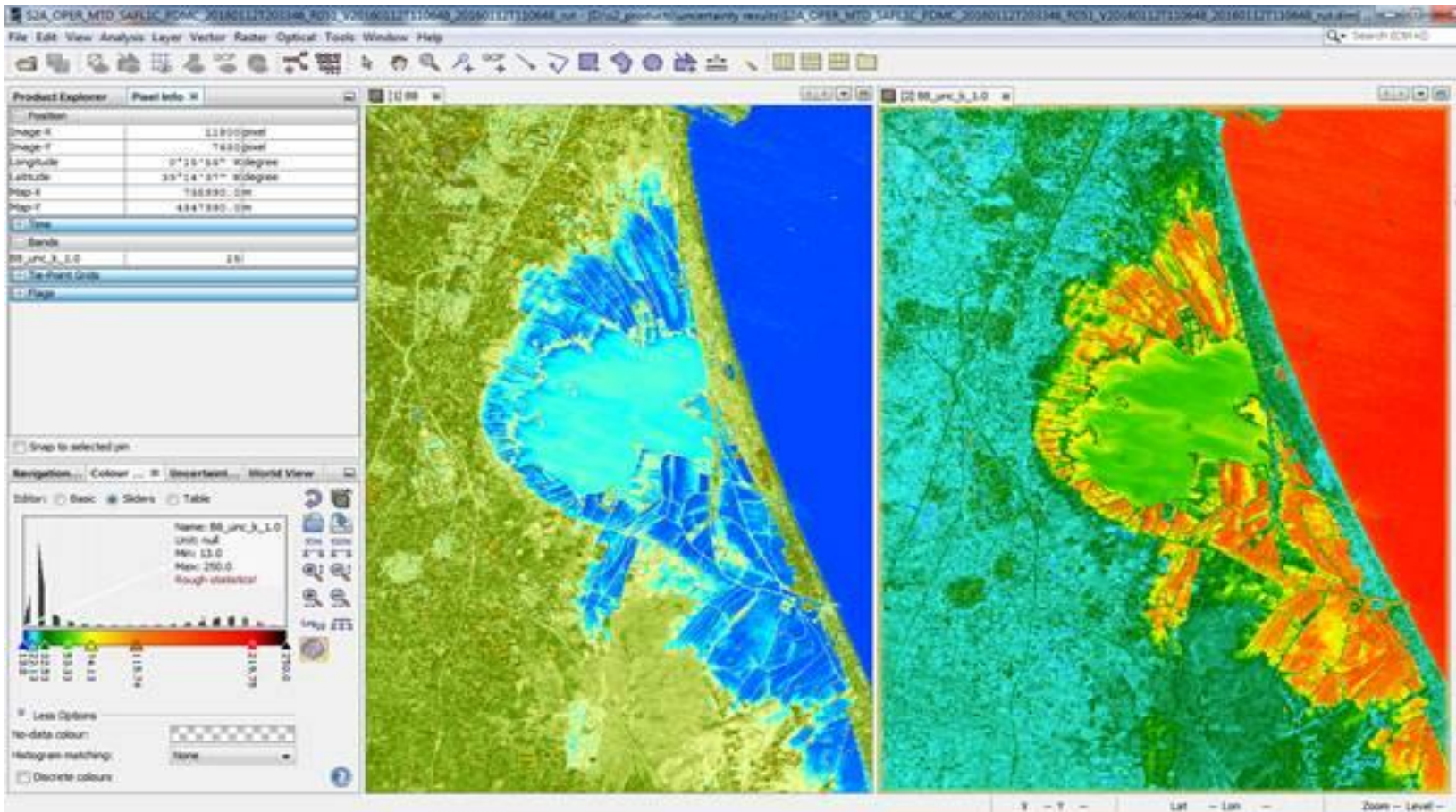


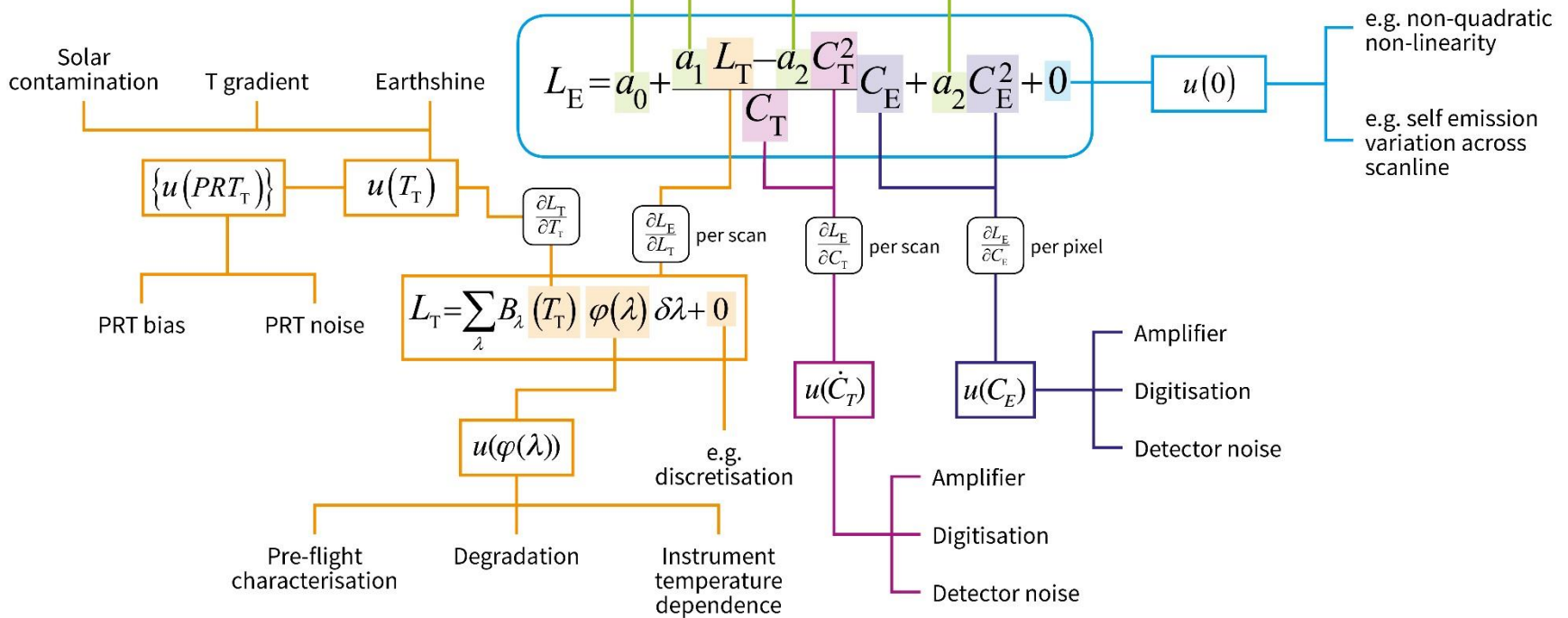
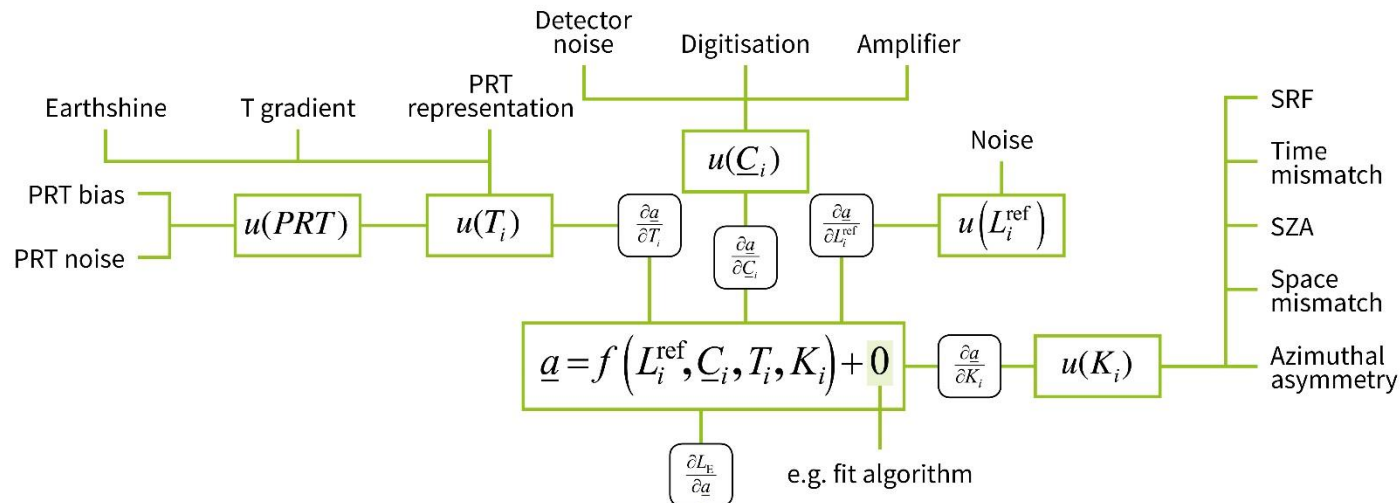
Traceability: Using matchups

$$L_E = a_0 + \frac{a_1 L_T - a_2 \dot{C}_T^2}{\dot{C}_T} C_E + a_2 C_E^2 + 0$$

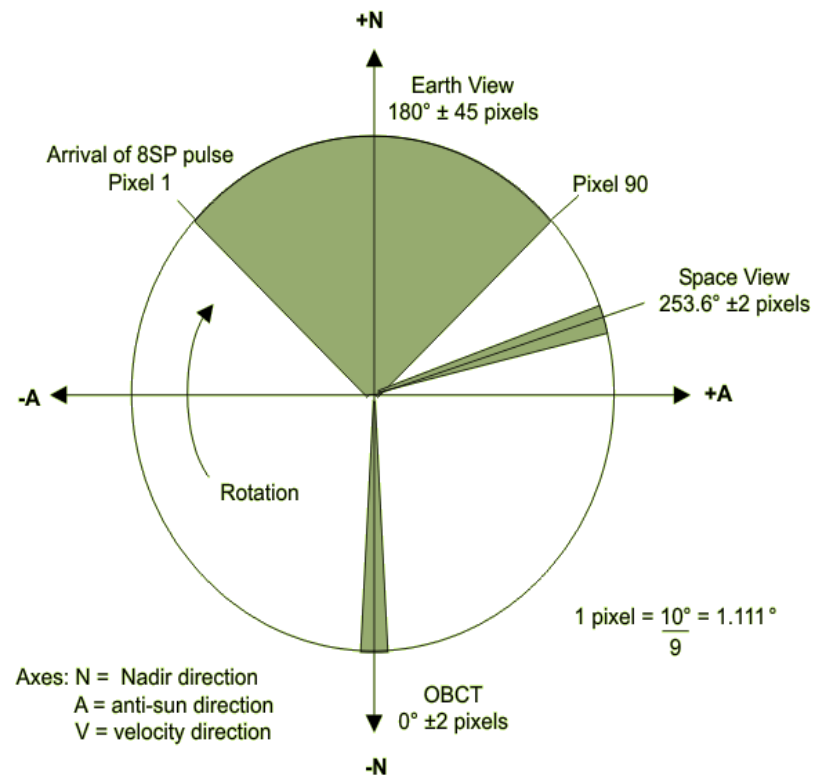
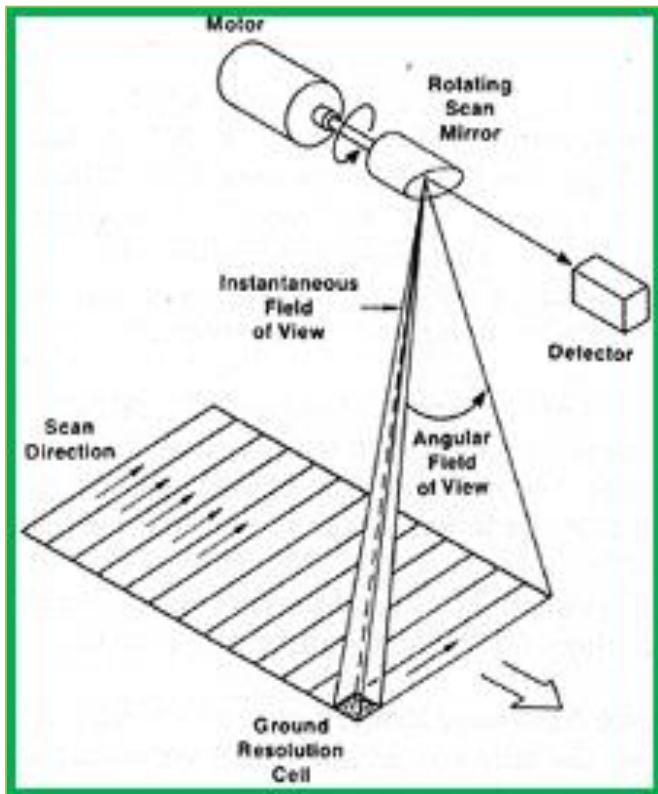


Uncertainty Analysis S2 Radiometric Uncertainty Tool



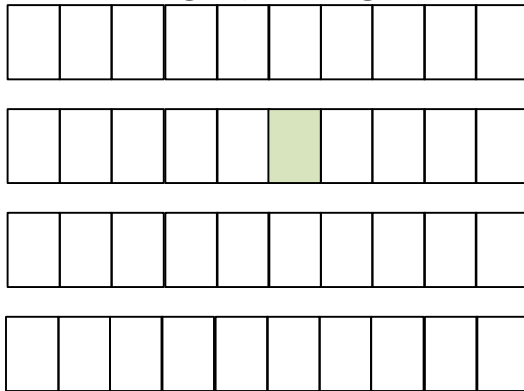


Error correlation

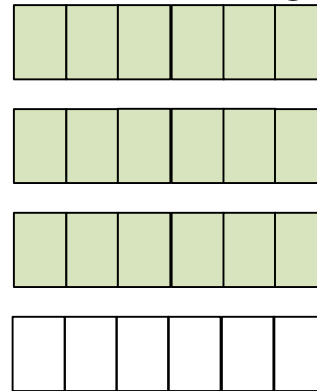


Error correlation between measured values

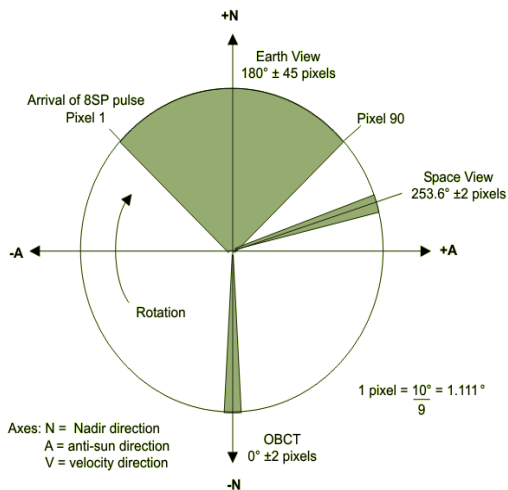
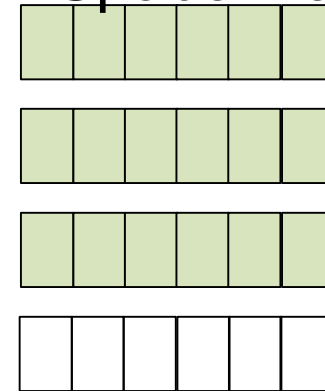
Earth view



Calibration target view

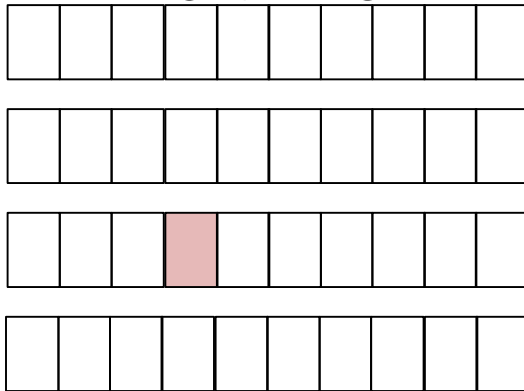


Space view

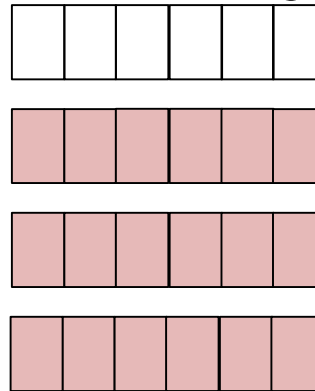


Error correlation between measured values

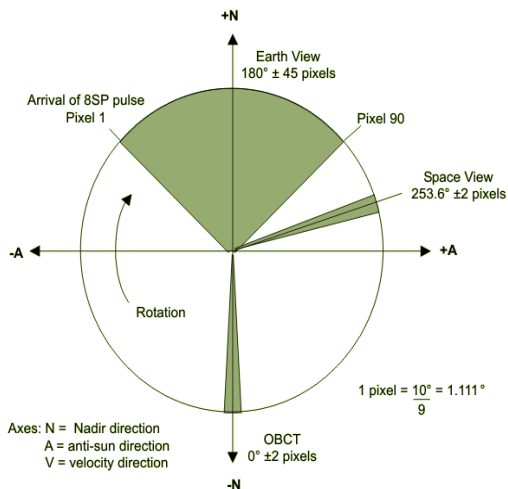
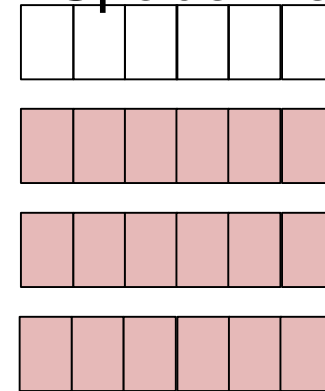
Earth view



Calibration target view

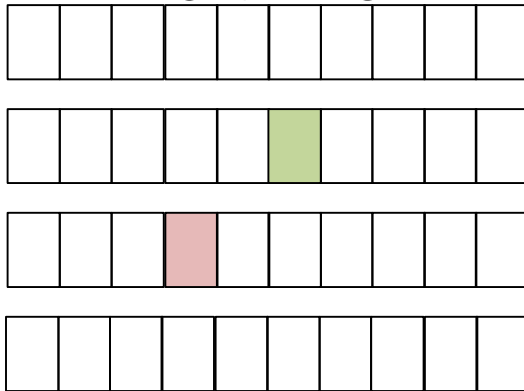


Space view

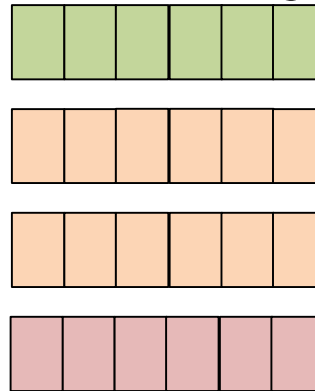


Error correlation between measured values

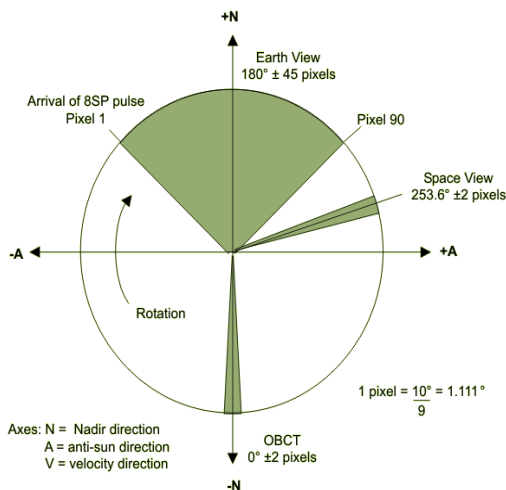
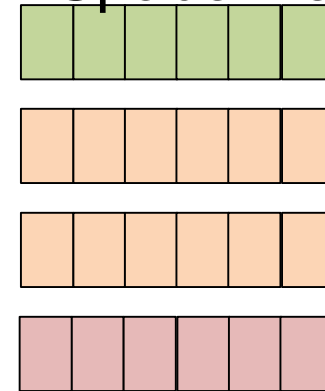
Earth view



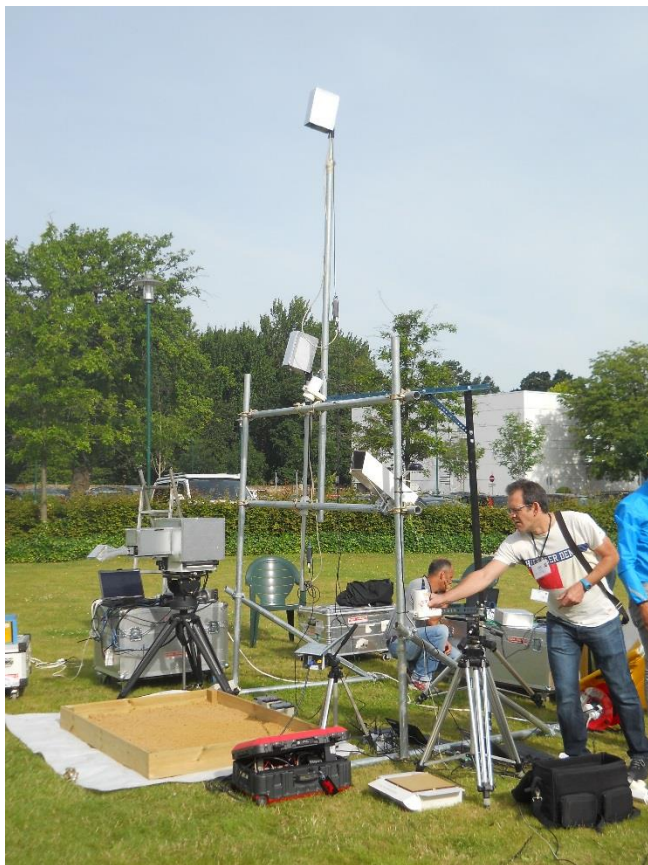
Calibration target view



Space view



Comparison



fiducial reference
temperature
measurements

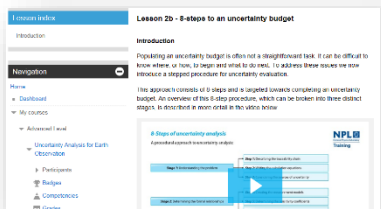
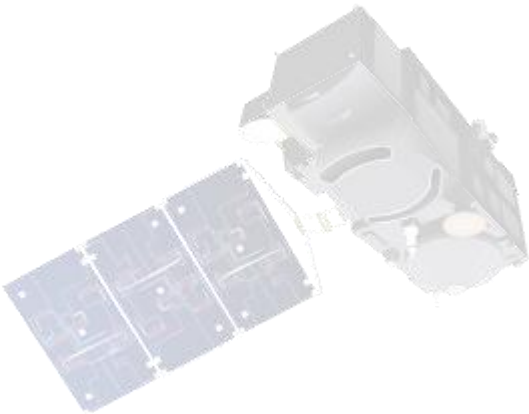
This presentation

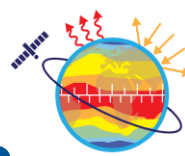


1. How world metrology achieves interoperability, stability and accuracy

2. How these principles can be applied to Earth Observation

3. Resources to help

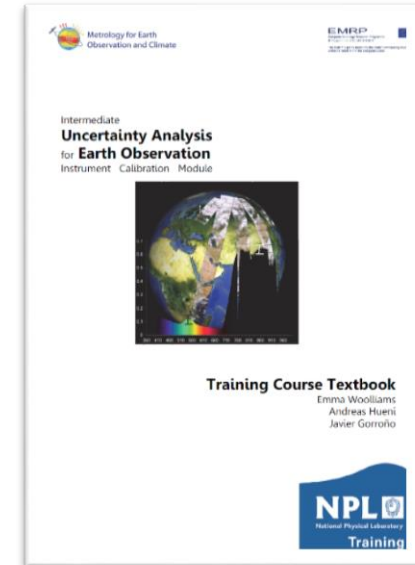




Training materials

- www.meteoc.org/outreach-training.html

- Text book “uncertainty analysis for EO instrument calibration”
- Videos of lectures (30-60 minutes each)



- www.npl.co.uk/e-learning

- Sign up for NPL’s e-learning courses
- Includes free “introduction to metrology” and “introduction to uncertainty”
- And (currently free) “Uncertainty Analysis for Earth Observation”

Screen shots from e-Course

Lesson index

Introduction

Navigation

Home

- Dashboard
- ▼ My courses
 - ▼ Advanced Level
 - ▼ Uncertainty Analysis for Earth Observation
 - ▶ Participants
 - 🏆 Badges
 - 🏆 Competencies
 - 📅 Grades
 - ▼ Module 1 - Introduction to the 8-steps of uncertai...
 - 📄 Lesson 2b - 8-steps to an uncertainty budget

-

8-Steps of uncertainty analysis
A procedural approach to uncertainty analysis:

Stage 1: Understanding the problem	Step 1: Describing the traceability chain
	Step 2: Writing the calculation equations
	Step 3: Considering the sources of uncertainty
Stage 2: Determining the formal relationships	Step 4: Creating the measurement models
	Step 5: Determining the sensitivity coefficients
	Step 6: Assigning uncertainties
Stage 3: Propagating the uncertainties	Step 7: Combining and propagating uncertainties
	Step 8: Expanding uncertainties

-

Lesson 7b - Applying the Full Form of the Law of Propagation of Uncertainty

Introduction

In part (a), we saw that, in cases where we can explicitly describe the correlation in the measurement model, only the first term of the Law of Propagation of Uncertainty is required. However, if this is not possible, the full form of the Law of Propagation of Uncertainty, shown below, is also needed.

$$u_c^2(y) = \sum_{i=1}^n c_i^2 u^2(x_i) + 2 \sum_{i=1}^{n-1} \sum_{j=i+1}^n c_i c_j u(x_i, x_j)$$

Applying the second term

In order to apply the second term in the Law of Propagation of Uncertainty we required two pieces of information:

- The relevant sensitivity coefficients
- The covariance of correlated input quantities

Since, we have already examined the different ways by which the sensitivity coefficients can be determined, we will focus our discussion towards determining the covariance of correlated input quantities. Here, we will see two ways by which this can be achieved:

- By calculating the covariance using an error model
- By estimating the covariance from experimental and modelled data

We will discuss these two methods in this lesson but before we do, let's see what would happen if we applied the Law of Propagation of Uncertainty to the two examples that we examined part (a) of this lesson. Doing so will give us an insight into the significance and meaning of the covariance term.

Administration

▶ Course administration

New material under development

- Question and answer based “shorts” (2 minute videos/single page texts)
- Focus on satellite Level 1 products

Examples:

- What do I need to know about an effect to propagate uncertainties?
- Can noise ever be correlated?
- How do we calculate the error correlation between measured values in different spectral bands?
- How do I know whether my uncertainties are right?

1 Concepts

- Chains and measurement function diagrams
- Propagating uncertainties
- Sensitivity coefficients
- Generic correlation

2 Practical implementation

- Noise
- Spectral uncertainties
- Calculating correlation
- Fitting

3 Validation and iteration

- Validating uncertainty budgets
- Discovering sensitivities and patterns

Resources to help...

- NPL
- MetEOC
- FIDUCEO
- FRM programme



Thank you



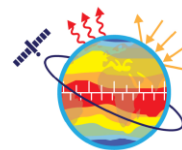
Department for
Business, Energy
& Industrial Strategy

FUNDED BY BEIS

The National Physical Laboratory is operated by NPL Management Ltd, a wholly-owned company of the Department for Business, Energy and Industrial Strategy (BEIS).



Centre for
EO Instrumentation



Metrology for Earth
Observation and Climate

MetEOC and MetEOC-2 were funded by EMRP
MetEOC-3 is funded under EMPIR



The EMPIR initiative is co-funded by the European Union's Horizon 2020 research and innovation programme and the EMPIR Participating States

FIDUCEO



FIDUCEO has received funding from the European Union's Horizon 2020 Programme for Research and Innovation, under Grant Agreement no. 638822



European Space Agency
Agence spatiale européenne